

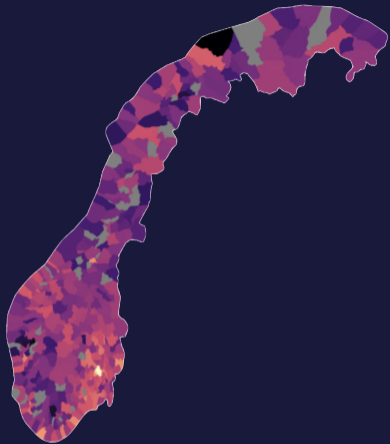
Frictions to intranational investment

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What this paper is about

- Strong gravity-like forces for *intranational* investment
- Exhaustive dataset and structural model
- (Plan to) run counterfactuals: Infrastructure improvements and spatial distribution of investments

Road map

1. Data and stylized facts
2. Related literature and background
3. Theory
4. Model calibration
5. Outlook: Counterfactuals

Stylized facts



→ Gravity classics: Home bias, size, distance, ...

Financial Asset Holdings

- Norwegian equity ownership data collected by the country's tax authority
 - Number of shares and their nominal value by owner, issuer
 - Annual data for years between 2004 to 2017
 - around 310,000 firms and around 1.02 million individual owners
- universe of domestic financial asset holdings
- in 2017: $\approx 20\%$ of nominal share capital foreign owned, value share of foreign assets $\approx 16\%$

Auxiliary datasets

- Location of individuals (Population register)
 - Firm location, age, subsidiaries, and plants by year (Firm register)
 - Firm sales, profits, and other balance sheet items (Database of tax filings)
- Spatial aggregation to county (*fylker*), municipality (*kommuner*) and basic statistical unit (*grunnkretser*)

Bilateral frictions

- Bilateral travel times and road distances by car: Open Source Routing Machine and Open Street Map data
- Population-weighted great circle distances
- Standards of written Norwegian: Nynorsk and Bokmål
- Municipality's ruling party
- Social Connectedness Index from Facebook
- Broadband coverage

Ad-hoc Gravity Estimation

$$A_{ij,t} = \exp(\mathbf{z}'_{ij,t}\beta_z + \lambda_{i,t} + \psi_{j,t})$$

- $A_{ij,t}$ nominal holdings of individuals from i in firms in j at time t
- $\mathbf{z}_{ij,t}$ vector of variables of interest and β_z the respective coefficients
- $\lambda_{i,t}$ and $\psi_{j,t}$ are origin \times year and destination \times year fixed effects
- Pseudo-Poisson Maximum Likelihood estimator

	Dependent variable: Nominal holdings $_{ij,t}$			
	(1)	(2)	(3)	(4)
log(Population Origin)	0.652*** (0.128)	- (-)	- (-)	- (-)
log(Population Destination)	0.734*** (0.122)	- (-)	- (-)	- (-)
Same municipality	2.610*** (0.456)	2.500*** (0.415)	2.695*** (0.471)	- (-)
log(Distance)	-1.057*** (0.065)	-1.271*** (0.066)	-0.977*** (0.900)	-0.081 (0.183)
log(Travel Time)	- (-)	- (-)	- (-)	-0.807*** (0.224)
Contiguity	- (-)	0.872*** (0.186)	0.922*** (0.294)	0.944*** (0.143)
Same language	- (-)	- (-)	0.907** (0.294)	0.157 (0.110)
Same ruling party	- (-)	- (-)	0.356* (0.140)	-0.006 (0.041)
Social connectedness	- (-)	- (-)	0.212*** (0.048)	0.385*** (0.063)
Fixed effects	-	<i>it, jt</i>	<i>it, jt</i>	<i>it, jt</i>
Sample size	2,493,176	2,493,176	2,493,176	2,486,847

Notes: Intercept in column (1) is suppressed. Standard errors clustered on origin, destination, and year in parenthesis. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

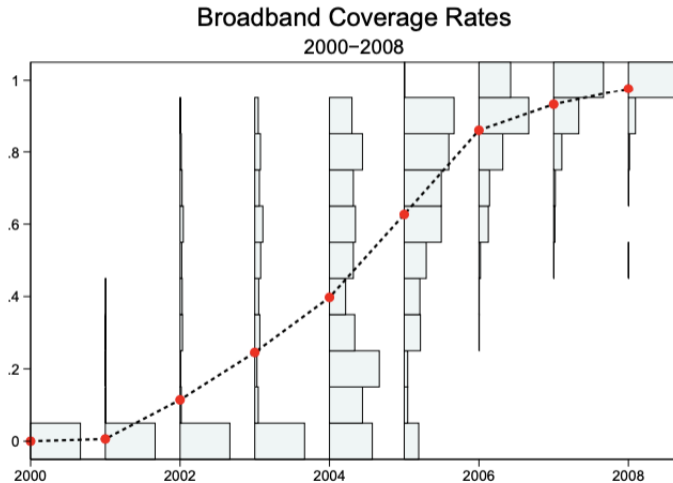
Ad-hoc Gravity Estimation

- Investments in home location about $\exp(2.61) \approx 13.6$ times higher than in comparable location
 - 10 % larger population of origin (destination) location associated with 6.5 % (7.3 %) larger investment
 - 1 % increase in distance decreases investments by about 1 %
 - Contiguity, language, political preferences, social connectedness matter
- Results similar to *international* frictions

Information frictions

- Frictions may be related to information or communication cost
 - Did better internet access reduce frictions and improve allocation of capital?
- Idea: Exploit variation in broadband roll-out over time and space

Broadband roll-out: Share of households covered



Source: Bhuller et al. 2013

	Dependent variable: Nominal holdings _{ij,t}		
	(1)	(2)	(3)
log(Travel Time)	-0.813*** (0.126)	-0.937*** (0.121)	- (-)
Contiguity	0.929*** (0.148)	0.896*** (0.152)	- (-)
Same language	0.072 (0.139)	0.073 (0.141)	- (-)
Same ruling party	0.041 (0.066)	0.033 (0.073)	- (-)
Social connectedness	0.373*** (0.066)	0.365*** (0.066)	- (-)
log(Travel Time) × Broadband coverage in origin	- (-)	0.126*** (0.041)	0.046** (0.020)
Fixed effects	<i>it, jt</i>	<i>it, jt</i>	<i>it, jt, ij</i>
Sample size	1,243,213	1,193,243	222,167

Notes: Standard errors clustered on origin, destination, and year in parenthesis.
*** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Related literature and context

Home and local bias in investment

- International: French & Poterba (1991), Coeurdacier and Rey (2013),...
- Intranational: Coval & Moskowitz (1999) — US fund holdings; Cumming & Dai (2010) — VC; Lin & Viswanathan, (2016), Guenther, Johan & Schweizer (2018) — crowd funding; Grinblatt & Keloharju (2001) — equity; Giroud (2013) — corporate investment

Structural models for gravity in international finance

- Martin & Rey (2004,2009); Okawa & van Wincoop (2012); Pellegrino et al. (2021)

Economic effects of the broadband expansion in Norway

- Bhuller et al. (2013), Akerman et al. (2019), Hvide et al. (2021)

Theory

Basic setup

- Economy comprised of J regions, indexed i, j
- Representative firms and representative investor in each region
- Capital only factor of production, equity only form of capital
- Firms' sales are subject to shocks, return to shares stochastic
- Investors may also invest in risk-free asset, denoted f

Investor problem

- Investor from i chooses number of shares from j to maximize lifetime utility

$$U_{i,t} = E \left[\sum_{s=0}^{\infty} \beta^s u(C_{i,t+s}) \right] \quad \text{s.t.}$$

$$C_{i,t+1} = W_{i,t+1} - \mathbf{a}_{i,t+1}' \mathbf{v}_{t+1} - a_{i,t+1}^f,$$

$$W_{i,t+1} = \mathbf{a}_{i,t}' \mathbf{s}_{t+1} + a_{i,t}^f R_{t+1}^f$$

- $\mathbf{a}_{i,t}' = [a_{i1,t}, \dots, a_{ij,t}, \dots, a_{iJ,t}]$ is vector of investments in assets $j = 1, \dots, J$
- $\mathbf{v}_t = [v_{1,t}, \dots, v_{j,t}, \dots, v_{J,t}]$ is vector of asset prices, $a_{i,1}^f$ risk-free investment
- $\mathbf{s}_t = [s_{1,t}, \dots, s_{j,t}, \dots, s_{J,t}]$ is vector of asset payoffs

Investor problem

- FOC w.r.t. $a_{i,t}^f$ and $a_{ij,t}$: $E[m_{i,t+1}R_{t+1}^f] = 1$ and $E[m_{i,t+1}S_{j,t+1}] = v_{j,t}$
- $m_{i,t+1} = \beta \frac{u'(C_{i,t+1})}{u'(C_{i,t})}$, stochastic discount factor (SDF), approximated as

$$m_{i,t+1} = \bar{\zeta}_{i,t} + \zeta_{i,t}R_{i,t+1}^W \quad \text{with} \quad R_{i,t+1}^W = \alpha_{i,t}^f R_{t+1}^f + \alpha'_{i,t} \mathbf{R}_{t+1}$$

- vector of portfolio shares $\alpha'_{i,t} = [\alpha_{i1,t}, \dots, \alpha_{ij,t}, \dots, \alpha_{iJ,t}]$ with elements $\alpha_{ij,t} = \frac{a_{ij,t}v_{j,t}}{A_{i,t}}$
 - vector of gross returns \mathbf{R}_{t+1} with elements $R_{j,t+1} = \frac{S_{j,t+1}}{v_{j,t}}$
 - value of the portfolio $A_{i,t} = \sum_{j=1}^J a_{ij,t}v_{j,t} + a_{i,t}^f$ with $\alpha_{i,t}^f$ share of risk-free asset
- several assumptions consistent with specification of SDF (Cochrane, 2000)

Investor problem

- Stochastic Euler equation (FOC w.r.t. $a_{ij,t}$) can be rewritten as

$$\frac{E_t [R_{j,t+1}]}{R^f} + \text{Cov}_t [m_{i,t+1}, R_{j,t+1}] = 1$$

- Using SDF, latter term can be written as $\text{Cov} [m_{i,t+1}, R_{j,t+1}] = \zeta_{i,t} \sum_{j'=1}^J \alpha_{ij',t} \sigma_{j,j'}$
- Then

$$\begin{aligned} \frac{1}{R^f} E_t [\mathbf{R}_{t+1}] + \zeta_{i,t} \boldsymbol{\Sigma}_t \boldsymbol{\alpha}_{i,t} &= \mathbf{1} \\ \iff \boldsymbol{\alpha}_{i,t} &= \frac{1}{-\zeta_{i,t}} \boldsymbol{\Sigma}_t^{-1} \left(\frac{1}{R^f} E_t [\mathbf{R}_{t+1}] - \mathbf{1} \right) \end{aligned}$$

- $\boldsymbol{\Sigma}_t$ covariance matrix of returns with elements $\sigma_{j,j'}$

- Information frictions similar to Okawa & van Wincoop (2012)
- Variance of asset j from investor i 's point of view:

$$\sigma_{jj}^i = \tau_{ij}^2 \sigma_{jj}$$

where σ_{jj} is the actual variance of R_j

Frictions — Generalization

- Now: Allowing arbitrary correlations between all regions' returns
- *Covariance* as perceived by investor i is distorted by information frictions:

$$\sigma_{jk}^i = \tau_{ij}\tau_{ik}\sigma_{jk}$$

where σ_{jk} denotes the actual covariance between R_j and R_k

- Covariance matrix of returns from i 's point of view is then

$$\Sigma^i = \mathbf{T}_i \Sigma \mathbf{T}_i$$

where \mathbf{T}_i is a diagonal matrix with element (i, j) equal to τ_{ij}

- Portfolio shares with i -specific covariance matrix then

$$\begin{aligned}\alpha_{i,t} &= \frac{1}{\zeta_{i,t} R_{t+1}^f} (\Sigma_t^i)^{-1} \left(E_t [\mathbf{R}_{t+1}] - \mathbf{R}_{t+1}^f \right) \\ &= \frac{1}{\zeta_{i,t} R_{t+1}^f} \mathbf{T}_i^{-1} \Sigma^{-1} \mathbf{T}_i^{-1} \left(E_t [\mathbf{R}_{t+1}] - \mathbf{R}_{t+1}^f \right)\end{aligned}$$

with $\tilde{\sigma}_{ij}$ being an element of Σ^{-1}

Bilateral investment with frictions

- Dropping time dimension, total bilateral investment then

$$\begin{aligned} A_{ij} &= \alpha_{ij} A_i \\ &= \frac{1}{\zeta_i R^f} \frac{1}{\tau_{ij}} c_{ij} A_i \end{aligned}$$

with
$$c_{ij} = \sum_k \frac{\tilde{\sigma}_{jk} (E[R_k] - R^f)}{\tau_{ik}}$$

- Gravity-style equation, featuring *two* bilateral terms
- Direct frictions τ_{ij}
- *Indirect* frictions related to the covariance of j 's return with all other regions' returns

Quantification

Quantification

- Solving for model-implied bilateral frictions
- $J \times J$ Euler equations
- Data on the bilateral share holdings, prices, and empirical distribution of profits

Euler equations

Rewrite $J \times J$ Euler equation as

$$E[R_j] - R^f = \sum_k^J \dot{\tau}_{ij} \dot{\tau}_{ik} \dot{\alpha}_{ik} \tilde{\sigma}_{jk} \quad \text{where}$$

$$\dot{\tau}_{ij} = \tau_{ij} \sqrt{\zeta_i R^f \alpha_i} \quad \text{and} \quad \dot{\alpha}_{ij} = \frac{\alpha_{ij}}{\alpha_i}$$

- Normalize domestic frictions: $\tau_{ii} = 1 \Rightarrow \dot{\tau}_{ii} = \sqrt{\zeta_i R^f \alpha_i}$ and $\tau_{ij} = \frac{\dot{\tau}_{ij}}{\dot{\tau}_{ii}}$
→ Calculate $J \times J$ scaled frictions $\dot{\tau}_{ij}$ using data on $E[R_j] - R^f$, $\dot{\alpha}_{ij}$

- Share prices v_j stock exchange, over-the-counter transactions, share emissions
 - extrapolation of missing share prices via industry \times municipality FEs and firm age
 - portfolio shares $\hat{\alpha}_{ij} = \frac{v_j a_{ij}}{\sum_k v_k a_{ik}}$
- Expected returns $E[R_j] = 1 + \frac{\bar{\pi}_j}{\bar{v}_j}$
 - $\bar{\pi}_j/\bar{v}_j$ sum of profits/market values of public firms in j , average over 10 years
- Covariance matrix of returns $\text{Cov} \left[\frac{\pi_j}{v_j}, \frac{\pi_k}{v_k} \right] \forall k, j$, computed over ten years

	Dependent variable: Model-implied frictions τ_{ij}	
	(1)	(2)
log(Travel Time)	0.519* (0.279)	0.666** (.325)
Same County	- (-)	-14.126*** (2.248)
Contiguity	- (-)	1.449 (5.531)
Same language	- (-)	0.506 (0.779)
Same ruling party	- (-)	1.412 (1.697)
Social connectedness	- (-)	-0.197 (0.741)
Sample size	323	323

Notes: Standard errors clustered on origin, destination, and year in parenthesis. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$

Outlook: Counterfactuals

Plan for Counterfactual Analysis

Quantify impact on spatial allocation of capital, efficiency of optimal portfolio, utility

- broadband roll-out
- geography, administrative and cultural barriers, transport infrastructure investments

Conclusions

- Gravity-type frictions to investment are not an international phenomenon
- Matter just as much for domestic capital markets
- Plan: Quantify impact of broadband access

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Firm problem and general equilibrium

- Firms choose inputs to maximize shareholder value net of the current cost of operating the firm
- $N_{j,t}$ number of firms in j at time t , market clearing for equity then

$$N_{j,t} = \sum_i a_{ij,t} \quad \Leftrightarrow \quad N_{j,t}V_{j,t} = \sum_i \alpha_{ij,t}A_{i,t}$$

- Equilibrium with free entry: willingness to pay for ownership equals cost of operating
- Equilibrium with fixed $N_{j,t}$: asset prices jointly determined by investor's Euler equation and market clearing condition